

PREREQUISITES PRACTICE PROBLEMS 1

Problem 1

Simplify

(1)
$$\frac{1}{2}(x - 2y)^2 - x^2 - \frac{3}{2}x \left(y - \frac{1}{2}\right)$$

(2)
$$\left(\frac{2}{3}x - 3\right) \left(\frac{2}{3}x + 3\right) - (1 - x)(1 + x)^2$$

(3)
$$\frac{\frac{1}{x+1} - \frac{1}{x}}{\frac{1}{x^2}}$$

(4)
$$\frac{x^3 + x^2 + x + 1}{x^2 - 1} - \frac{9x^2 + 6x + 1}{3x^2 - 3x + x - 1} + \frac{2}{x}$$

Problem 2

Factor

(5)
$$16x^3 + 8x^2 + x$$

(6)
$$x^6 - \frac{1}{9}x^2$$

(7)
$$3y^3 + 2y^2 - y$$

(8)
$$2x^3 - 2 + 2x - 2x^2$$

(9)
$$x^4 + 4$$

Problem 3

Solve the following equations/inequalities

(10)
$$\frac{2}{3}(x - 1) + 2x = 1 + \frac{8}{3}x$$

(11)
$$3x^3 - 4x^2 - x = 0$$

(12)
$$\frac{x}{1-x} - \frac{1}{2} = \frac{2-x}{x}$$

(13)
$$\sqrt{x^2 - 7} = 3$$

(14)
$$x^5 + 1 = 0$$

(15)
$$\frac{3-x}{9x^2-2x} > 0$$